

Permutations:

10 n - # to choose from

3 r - # many you choose

Formula:

$$\frac{n!}{(n-r)!}$$

Example: You have 10 numbers 0-9

n^r → make a lock combination with 3 numbers.

$$10^3$$

$$10 \cdot 10 \cdot 10$$

$$\frac{10!}{7!}$$

$$\frac{10 \cdot 9 \cdot 8 \cdot \cancel{7} \cdot \cancel{6} \cdot \cancel{5} \cdot \cancel{4} \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{1}}{\cancel{7} \cdot \cancel{6} \cdot \cancel{5} \cdot \cancel{4} \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{1}}$$

Combinations: The number of ways to select items from a larger set.

Example: Choose a committee of 3 students from 5 volunteers.

Formula:

$${}^nC_r = \frac{{}^nP_r}{r!} = \frac{n!}{r!(n-r)!}$$

MATH

PRB

$${}^nC_r \leq {}^nC_r$$

$${}^nP_r =$$

$$\frac{5!}{3! \cdot (2)!}$$

$$\frac{5 \cdot 4 \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{1}}{\cancel{3} \cdot \cancel{2} \cdot \cancel{1} (2 \cdot 1)} = \frac{20}{2}$$

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Counting with Repetition:

Order does not matter. Things can be used more than once.

$$\frac{n!}{(m!)(t!)}$$

n - total things

Example: How many code words can be made using the word SUCCESS?

m - repeating
 t - letters

$m = 3$ (S)
 $t = 2$ (C)

$$\frac{7!}{(3!)(2!)} = 420$$

Factorial: The product of an integer and all integer below it.

$$\text{Example : } 5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

Symbol - $n!$

$$20! = 20 \cdot 19 \cdot 18 \cdot \dots \cdot 2 \cdot 1$$

